

Changing systemic risks in Chinese bond market and risk premia in Treasury yields (Work in progress)

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Quantitative Easing and Financial (In)stability, Tokyo Meeting

January 31, 2018

Outline

- 1 Introduction
- 2 Literature Review
- 3 Data
- 4 An AFENS model for Treasury yield curve
- 5 An AFENS model for multiple yield curves (in progress)
- 6 Estimation results
- 7 Conclusion (for now)

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Introduction

■ The big questions

- Debt crisis: will China follow US and Europe?
- Fiscal stimulus in China: an alternative QE, for growth or for bust?
- Understanding evolvement of systemic risks in Chinese financial market

■ A special perspective

- Changes in the systemic risks reflected in bond yields
- Comparative study of bond yields in a no-arbitrage framework on Treasury vs. Chengtou bonds (quasi municipal government bonds)

Three trends of Chinese debt market: 2009 - 2017

- First, the main driving force for overall debt issuance and outstanding volume is public sector debt (state-owned enterprises and local government related).

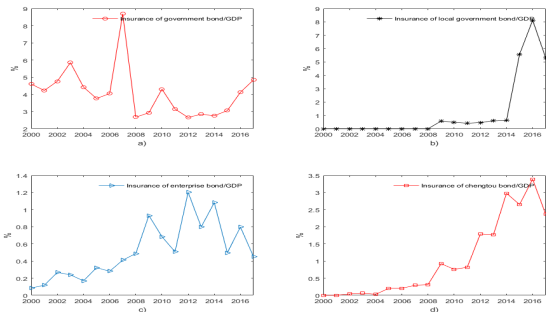


Figure 1: Bond Issuance as percentage of GDP (2000 - 2017)

Three trends of Chinese debt market: 2009 - 2017

- A pertaining structural imbalance of fiscal power and responsibility between central and local governments.

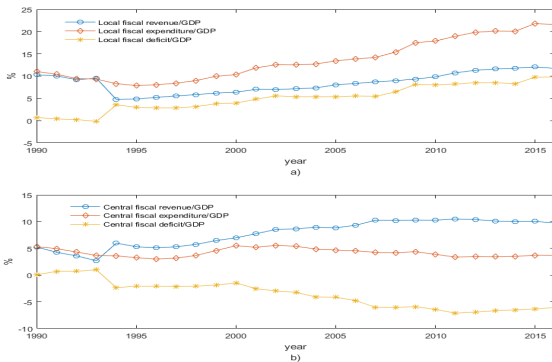


Figure 2: Fiscal deficit of local and central governments (1990-2016)

Three trends of Chinese debt market: 2009 - 2017

- Since 2015, legal issuance of local government bonds hand in hand with the debt replacement program lead to increased transparency but skyrocketing scale.

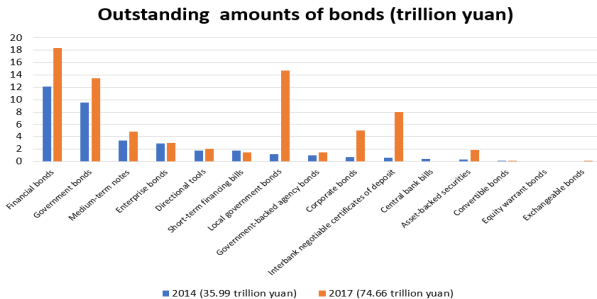


Figure 3: Outstanding debt volume: 2014 vs. 2017

Three trends of Chinese debt market: 2009 - 2017

Second, as debt grows, credit structure deteriorates, most evident from Chengtou bond with high degree of marketization.

Table 1: Structure of Chengtou bonds with different credit ratings

a: Issuer's credit rating of Chengtou bond issuance (Percentage in volume)									
Level	2009	2010	2011	2012	2013	2014	2015	2016	2017
AAA	50.92%	28.61%	21.46%	14.62%	24.01%	22.08%	28.19%	31.09%	41.68%
AA+	28.42%	40.54%	39.49%	35.24%	30.71%	31.32%	34.25%	32.28%	27.11%
AA	19.99%	29.86%	35.33%	48.35%	44.59%	46.35%	37.34%	36.62%	30.90%
AA-	0.67%	0.99%	3.72%	1.79%	0.69%	0.24%	0.22%	0.02%	0.31%
b: Bond's credit rating of Chengtou bond issuance (Percentage in volume)									
Level	2009	2010	2011	2012	2013	2014	2015	2016	2017
AAA	46.76%	28.66%	27.47%	17.23%	19.77%	22.10%	27.57%	23.92%	29.81%
AA+	37.41%	46.34%	39.91%	36.32%	34.36%	28.06%	32.43%	30.09%	28.80%
AA	15.11%	23.78%	31.76%	43.92%	44.15%	49.10%	37.76%	42.93%	37.70%
AA-	0.72%	1.22%	0.86%	2.53%	1.73%	0.74%	2.24%	3.06%	3.68%
c: Bond's credit rating of outstanding Chengtou bond (Percentage in total volume)									
Level	2009	2010	2011	2012	2013	2014	2015	2016	2017
AAA	63.62%	41.24%	36.75%	25.77%	30.71%	29.05%	31.40%	28.08%	23.14%
AA+	26.93%	38.85%	37.41%	34.98%	33.46%	28.43%	25.18%	25.19%	35.77%
AA	8.99%	19.47%	25.31%	37.83%	35.38%	42.31%	39.85%	43.00%	37.06%
AA-	0.46%	0.44%	0.53%	1.41%	0.45%	0.21%	3.56%	3.73%	4.02%

Data source: Wind Database



Three trends of Chinese debt market: 2009 - 2017

- Third, as a tip of the iceberg of public sector debt, credit risks began to be gradually priced into Chengtou bond yield spreads.

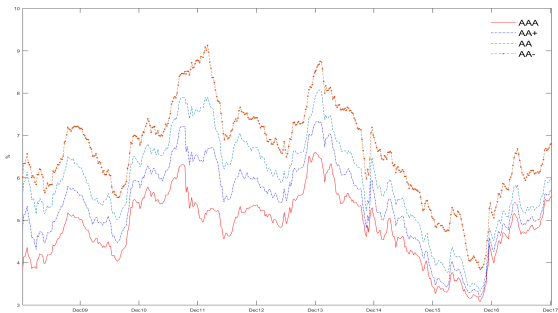


Figure 4: Chengtou bond spread (5-year yield spreads of various ratings)

Introduction

■ A specific question

To which extent the public sector debt problem exposes China's fiscal and financial system to risks?

■ Steps to approaching the answer with bond yield data

- 1) Constructing systemic bond risk measures from Chengtou bond spreads (liquidity risk, credit risk, maturity risk)
- 2) Modeling Joint dynamics of systemic bond risks and Treasury yields with no-arbitrage restrictions
- 3) How do systemic bond risks evolve?
- 4) How do systemic bond risks affect Treasury yield curve and vice versa?
- 5) Pricing of systemic bond risks in Treasury bond risk premia.

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Literature Review

1) Accumulation of local governmental debt and systemic risks

龚强(2011) literature survey, 徐高& 王艺伟(2013) on detailed development of chengtou bonds, 范剑勇& 莫家伟(2014) on local debt, land market and regional industrial growth with distortion and systemic risks, 郭玉清(2011) on financial stability linked to non-performing bank loans of LGFVs

Literature Review

2) Determinants of chengtou bond spreads and the relationship with risk free rates

- Ang et. al (2016), panel data analysis on chengtou bond spreads across regions. Risk factors: real estate market, degree of corruption
- Relationship between credit spread and risk free yields: Merton (1974), Longstaff & Schwartz (1995) , Duffee(1998) , etc.
- Negative relationship found between corporate bond spreads and Treasury yields (Dai and Sun, 2011, Wang et al, 2014) within a reduced-form model

Literature Review

3) Macro-finance study on Treasury yield curves

- Interaction between macro fundamentals and yield factors: Taylor (1993), Ang & Piazzesi (2003), Diebold et al. (2005), etc.
- Dai & Philippon (2004): US fiscal deficit as a macro factor for yield curve modeling

Literature Review

■ What we do in this paper

- Using price information to investigate systemic risks caused by local public debt accumulation and their impacts on Treasury yields: quick, market expectation
- Jointly modeling multiple Chengtou yield curves with Treasury yield curve in a parsimonious no-arbitrage framework (in progress)

The framework is derived from

- Affine arbitrage-free Nelson-Siegel (AFNS) term structure model (Christensen, et al., 2009)
- AFNS in discrete time (Hong, Niu and Zeng, 2015)
- Affine arbitrage-free extended Nelson-Siegel (AFENS) model with additional factors beyond the NS three yield factors (Li, Niu and Zeng, 2012).

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Data description

- **Sample period:** beginning of 2009 to the end of 2017
- **Frequency:** weekly
- **Treasury yields:** interbank spot rate 1-10 years
- **Chengtou yields of AAA, AA+, AA, AA- ratings:** interbank 1-7 years
- **Data source:** WIND financial database

Data description

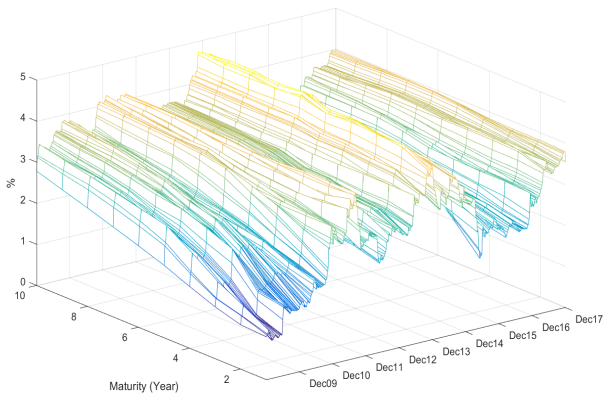


Figure 5: Treasury yield curve in China (2009 - 2017)



Risk factor proxy of Chengtou spreads

Liquidity factor (Lq): Average spread between AAA Chengtou yields and Treasury yields $Lq_t = \bar{y}_t^{AAA} - \bar{y}_t^T$

Credit risk factor (Cr):

- 1) Average spreads between lower rating Chengtou yields and AAA Chengtou yields: $S_t^{AAA-} = \bar{y}_t^{AAA-} - \bar{y}_t^{AAA}$, S_t^{AA+} , S_t^{AA} , S_t^{AA-}
- 2) Residual from the regression of S_t^{AAA-} , S_t^{AA+} , S_t^{AA} and S_t^{AA-} on Lq_t
- 3) Extract the first principle component from the residuals of step 2)

Risk factor proxy of Chengtou spreads

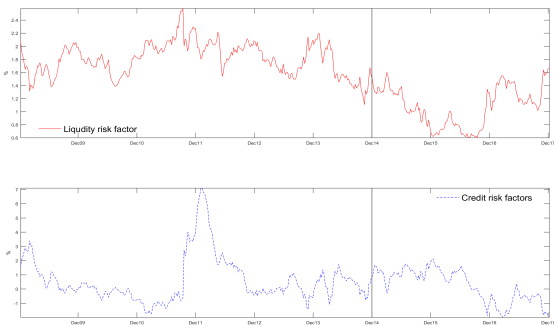


Figure 6: Two risk proxies constructed from Chengtou spreads

Break test on the risk factors around the end of 2014

Table 2: Break test on the risk factors

Chow Breakpoint Test: 12/31/2014				
Null Hypothesis: No breaks at specified breakpoints				
Varying regressors: All equation variables				
Equation Sample: 1/16/2009-1/05/2018				
Liquidity factor	F-statistic	3.750	Prob. F(6,454)	0.001
	Log likelihood ratio	22.540	Prob. Chi-Square(6)	0.001
	Wald Statistic	22.499	Prob. Chi-Square(6)	0.001
Credit risk factor	F-statistic	1.686	Prob. F(6,454)	0.123
	Log likelihood ratio	10.272	Prob. Chi-Square(6)	0.114
	Wald Statistic	10.118	Prob. Chi-Square(6)	0.120

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Building blocks

- State variables:

NS factors $X_t^{NS} = [L_t, S_t, C_t]$ of the Treasury yields and the chengtou risk factor $Sp_t = [Lq_t, Cr_t]$

- Short rate equation

$r_t = \delta_0 + \delta_1' X_t$ where δ_0 is a scale and $\delta_1 = \left[1, \frac{1-e^{-\lambda}}{\lambda}, \frac{1-e^{-\lambda}}{\lambda} - e^{-\lambda}, \delta_1^{Sp} \right]'$.

- Dynamics of factors under the physical measure

$$X_t = \mu + \Phi X_{t-1} + v_t \quad v_t \sim N(0, \Omega) \quad (1)$$

where $X_t = [X_t^{NS}, Sp_t]'$.

Building blocks

■ Dynamics of factors under the risk-neutral measure

$$\begin{bmatrix} X_t^{NS} \\ Sp_t \end{bmatrix} = \begin{bmatrix} \mu^{NSQ} \\ \mu^{SpQ} \end{bmatrix} + \begin{bmatrix} \Phi^{NSQ} & 0 \\ \Phi^{SpNSQ} & \Phi^{SpQ} \end{bmatrix} \begin{bmatrix} X_{t-1}^{NS} \\ Sp_{t-1} \end{bmatrix} + v_t^Q \quad v_t^Q \sim N(0, \Omega) \quad (2)$$

$$\text{where } \mu^{NSQ} = [\mu^{LQ} \ 0 \ 0]', \Phi^{NSQ} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & e^{-\lambda} & \lambda e^{-\lambda} \\ 0 & 0 & e^{-\lambda} \end{bmatrix}$$

Building blocks

■ Treasury yield curve determination

$$\begin{aligned}
 y_t^n &= a_n^{NS} + b_n^{NS'} X_t^{NS} \\
 &= -\frac{1}{n} \left(A_n^{NS} + B_n^{NS'} X_t^{NS} \right)
 \end{aligned} \tag{3}$$

where

$$\begin{cases}
 A_{n+1}^{NS} &= A_n^{NS} + B_n^{NS'} \mu^{NSQ} + \frac{1}{2} B_n^{NS'} \Omega^{NS} B_n^{NS} + A_1^{NS} \\
 B_{n+1}^{NS'} &= B_n^{NS'} \Phi^{NSQ} + B_1^{NS'}
 \end{cases}, \tag{4}$$

$$A_1^{NS} = -\delta_0^{NS} \text{ and } B_1^{NS} = -\delta_1^{NS}.$$

Building blocks

- Yield decomposition: expectation and risk premium

$$\bar{y}_t^n = -\frac{1}{n} (\bar{A}_n + \bar{B}_n' X_t) \quad (5)$$

where

$$\begin{cases} \bar{A}_{n+1} = \bar{A}_n + \bar{B}_n' \mu + \frac{1}{2} \bar{B}_n' \Omega \bar{B}_n - \delta_0 \\ \bar{B}_{n+1} = \Phi' \bar{B}_n - \delta_1 \end{cases}$$

$$\begin{aligned} RP_t^n &= y_t^n - \bar{y}_t^n \\ &= -\frac{1}{n} (A_n^{NS} + B_n^{NS'} X_t^{NS}) + \frac{1}{n} (\bar{A}_n + B_n' X_t) \end{aligned}$$

Econometric representation

The econometric representation of the model given by Equations (1 -5) can be expressed as follows,

$$\begin{cases} Y_t = A + BX_t + \epsilon_t & \epsilon_t \sim N(0, \sigma^2 I) \\ X_t = \mu + \Phi X_{t-1} + v_t & v_t \sim N(0, \Omega) \end{cases} \quad (6)$$

where Y_t is the column vector containing the yields of government bonds, A and B are determined by the parameters μ^{L^Q} , λ and Ω .

Estimation method: MCMC

Denote $\Theta_1 = \{\mu^{L^Q}, \lambda, \sigma\}$, $\Theta_2 = \{\mu, \Phi, \Omega\}$, we apply MCMC method to estimate the model. The main steps of the MCMC estimation are shown as follows,

- Given $\Theta_1^{(s-1)}$, $\Theta_2^{(s-1)}$ and the observable data Y_t , drawing $X_t^{(s)}$
- Given $\Theta_1^{(s-1)}$, $\Theta_2^{(s-1)}$, $X_t^{(s)}$, and the observable data Y_t , drawing $\Theta_2^{(s)}$
- Given $\Theta_1^{(s-1)}$, $\Theta_2^{(s)}$, $X_t^{(s)}$, and the observable data Y_t , drawing $\Theta_1^{(s)}$

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The measurement equation representation

$$\left\{ \begin{array}{l} y_{t,n}^T = a_n^T + b_n^{NS'} X_t^{NS} \\ y_{t,n}^{AAA} = a_n^{AAA} + b_n^{NS'} X_t^{NS} + b_n^{AAA'} Sp_t + c_n^{AAA'} f_t^{AAA} \\ y_{t,n}^{AA+} = a_n^{AA+} + b_n^{NS'} X_t^{NS} + b_n^{AA+'} Sp_t + c_n^{AA+'} f_t^{AA+} \\ y_{t,n}^{AA} = a_n^{AA} + b_n^{NS'} X_t^{NS} + b_n^{AA'} Sp_t + c_n^{AA'} f_t^{AA} \\ y_{t,n}^{AA-} = a_n^{AA-} + b_n^{NS'} X_t^{NS} + b_n^{AA-' } Sp_t + c_n^{AA-' } f_t^{AA-} \end{array} \right. \quad (7)$$

where Sp_t contains the common risk factors which are spanned for chengtou yield curve but unspanned for treasury yield curve, and f_t^{AAA} , f_t^{AA+} , f_t^{AA} and f_t^{AA-} are individual risk factors of chengtou yields with various credit ratings.

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Full sample estimation of model parameters

Table 3: Parameters estimation under risk-neutral and physical measures

Θ_1		μ_L^Q	λ	σ		
		-4.85E-07 ***	8.15E-03 ***	9.18E-06 ***		
Θ_2		L	S	C	Lq	Cr
μ		3.34E-05 ***	-2.32E-05	-9.94E-05 **	-2.86E-05 **	1.53E-04 **
		0.959 ***	-0.003	0.003	0.027	0.001
		0.029	0.987 ***	0.011	-0.031	-0.009
Φ		0.115	0.016	0.930 ***	-0.119 *	-0.010
		0.050 ***	0.007	0.008 **	0.944 ***	0.001
		-0.252 ***	-0.018	-0.009	0.333 **	0.971 ***
		3.63E-10 ***	-2.15E-10 ***	-8.01E-10 ***	4.99E-11 **	-2.34E-10 ***
		-2.15E-10 ***	9.16E-10 ***	-3.89E-10 **	3.71E-11	-6.29E-11
Ω		-8.01E-10 ***	-3.89E-10 **	5.01E-09 ***	-3.05E-10 ***	1.13E-09 ***
		4.99E-11 **	3.71E-11	-3.05E-10 ***	2.53E-10 ***	-7.84E-10 ***
		-2.34E-10 ***	-6.29E-11	1.13E-09 ***	-7.84E-10 ***	3.76E-09 ***

Note: This table presents the parameters estimation by MCMC method. *, ** and *** represent significantly rejecting the null hypothesis at levels of the 10%, 5% and 1%, respectively.

Goodness of fit for Treasury yields

Table 4: Goodness of fit for Treasury yields

Maturity (Year)	Mean of error	Std of error	MAE	RMSE
1-y	0.53	3.87	3.02	3.90
2-y	-0.95	6.08	4.61	6.15
3-y	-0.51	4.44	3.33	4.46
4-y	-0.10	3.62	2.71	3.62
5-y	3.16	4.73	4.76	5.68
6-y	-1.68	4.42	3.63	4.73
7-y	-0.47	3.88	3.20	3.90
8-y	-0.52	2.90	2.20	2.94
9-y	0.25	2.23	1.66	2.24
10-y	0.27	3.57	2.74	3.58
Average	0.00	3.97	3.19	4.12

Note: The unit is bp.

Factor dynamics (full sample)

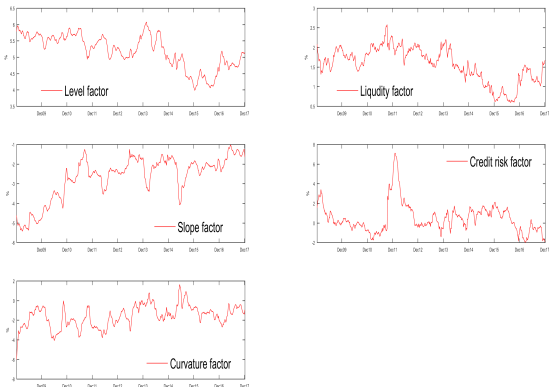


Figure 7: Factor dynamics (full sample)

Comparison on subsample 1 (2009-2014) and subsample 2 (2015 – 2017)

Table 5: Estimation of model parameters in the state VAR (2009-2014)

	L	S	C	Lq	Cr
μ	4.32E-05 **	2.36E-05	-1.47E-04 *	1.15E-05	2.19E-05
	0.954 ***	-0.003	0.004	-0.001	0.003
	-0.005	0.986 ***	0.015	-0.058	-0.006
Φ	0.147	0.017	0.920 ***	-0.012	-0.015
	0.017	0.004	0.012 **	0.935 ***	0.003
	-0.157 *	-0.007	-0.017	0.351 ***	0.967 ***
	2.86E-10 ***	-1.97E-10 ***	-5.72E-10 ***	4.18E-11	-2.01E-10 *
	-1.97E-10 ***	9.55E-10 ***	-3.71E-10 *	4.72E-11	-1.80E-10
Ω	-5.72E-10 ***	-3.71E-10 *	4.69E-09 ***	-3.95E-10 ***	1.52E-09 ***
	4.18E-11	4.72E-11	-3.95E-10 ***	2.74E-10 ***	-8.72E-10 ***
	-2.01E-10 *	-1.80E-10	1.52E-09 ***	-8.72E-10 ***	4.50E-09 ***

Note: This table presents the parameters estimation by MCMC method. *, ** and *** represent significantly rejecting the null hypothesis at levels of the 10%, 5% and 1%, respectively.

Comparison on subsample 1 (2009-2014) and subsample 2 (2015 - 2017)

Table 6: Estimation of model parameters in the state VAR (2015-2017)

	L	S	C	Lq	Cr
μ	1.09E-04 ***	-2.98E-05	-4.15E-04 ***	-7.25E-05 ***	2.50E-04 ***
	0.876 ***	-0.001	0.024 *	0.056	-0.017
	0.025	0.951 ***	0.012	-0.045	-0.029 *
Φ	0.502 **	0.042	0.861 ***	-0.332	0.040
	0.125 **	0.006	0.006	0.822 ***	-0.019 ***
	-0.446 ***	-0.057	-0.006	0.645 ***	1.010 ***
	5.63E-10 ***	-2.73E-10 ***	-1.36E-09 ***	4.31E-11	-2.43E-10 **
	-2.73E-10 ***	1.13E-09 ***	-8.19E-10 ***	4.47E-11	3.31E-11
Ω	-1.36E-09 ***	-8.19E-10 ***	6.97E-09 ***	-1.34E-10	4.91E-10
	4.31E-11	4.47E-11	-1.34E-10	1.98E-10 ***	-5.85E-10 ***
	-2.43E-10 **	3.31E-11	4.91E-10	-5.85E-10 ***	2.36E-09 ***

Note: This table presents the parameters estimation by MCMC method. *, ** and *** represent significantly rejecting the null hypothesis at levels of the 10%, 5% and 1%, respectively.

Impulse responses of yields to liquidity shock (2009-2014)

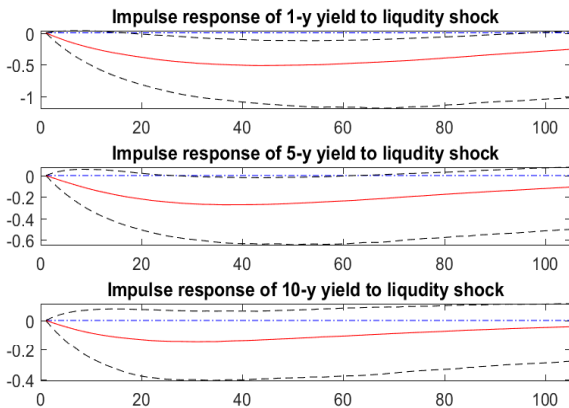


Figure 8: Impulse responses of yields to liquidity shock (2009-2014)

Impulse responses of yields to liquidity shock (2015-2017)

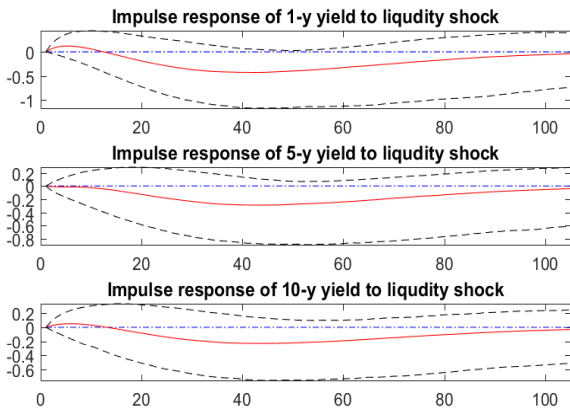


Figure 9: Impulse responses of yields to liquidity shock (2015-2017)

Impulse responses of yields to credit risk shock (2009-2014)

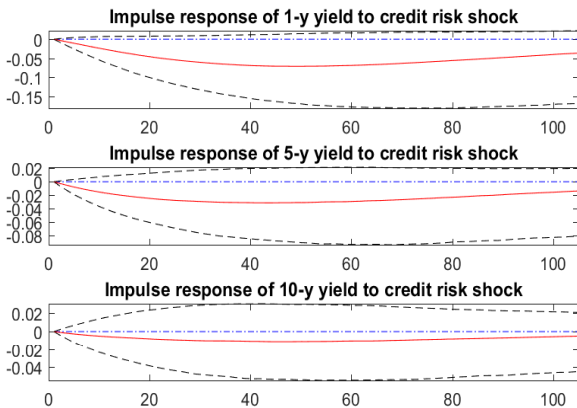


Figure 10: Impulse responses of yields to credit risk shock (2009-2014)

Impulse responses of yields to credit risk shock (2015-2017)

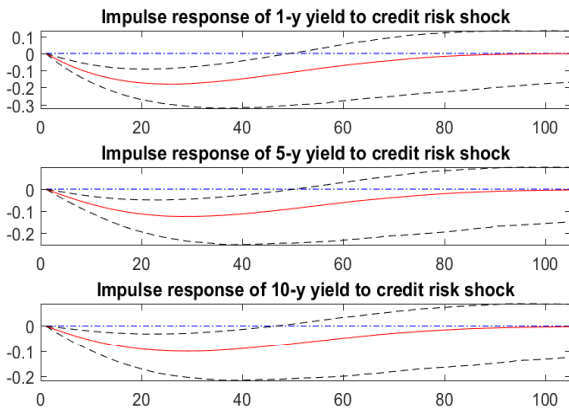


Figure 11: Impulse responses of yields to credit risk shock (2015-2017)

Impulse responses of yield expectation and risk premia to liquidity shock (2009-2014)

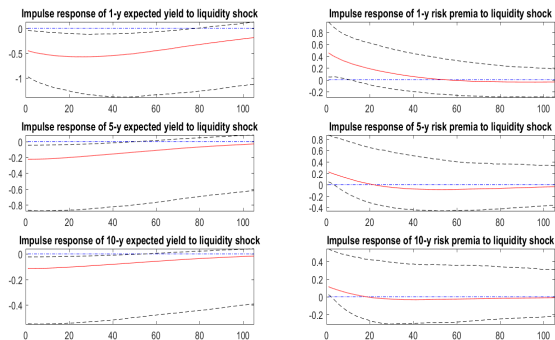


Figure 12: Impulse responses of yield expectation and risk premia to liquidity shock (2009-2014)

Impulse responses of yield expectation and risk premia to liquidity shock (2015-2017)

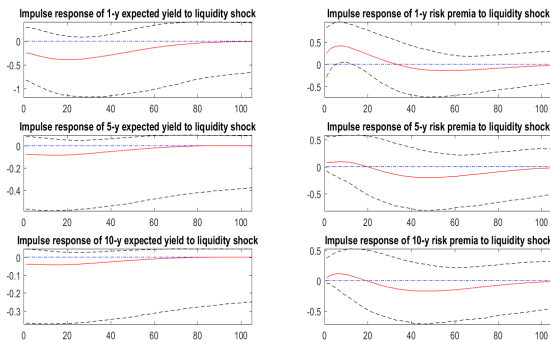


Figure 13: Impulse responses of yield expectation and risk premia to liquidity shock (2015-2017)

Impulse responses of yield expectation and risk premia to credit risk shock (2009-2014)

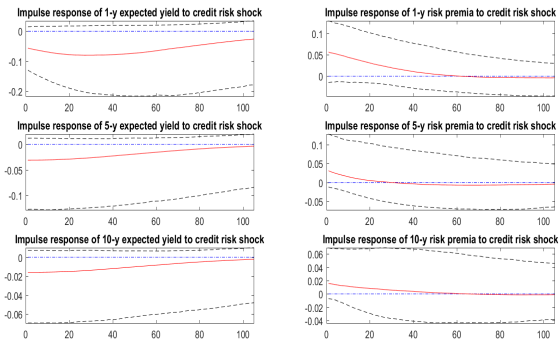


Figure 14: Impulse responses of yield expectation and risk premia to credit risk shock (2009-2014)

Impulse responses of yield expectation and risk premia to credit risk shock (2015-2017)

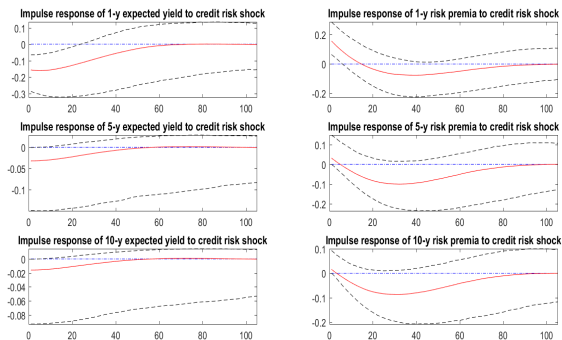


Figure 15: Impulse responses of yield expectation and risk premia to credit risk shock (2015-2017)

Impulse responses of liquidity risk and credit risk (2009-2014)

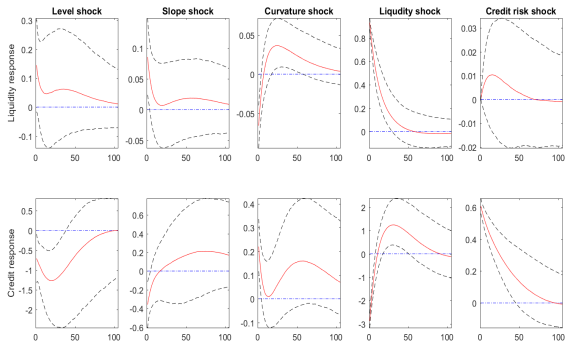


Figure 16: Impulse responses of liquidity risk and credit risk (2009-2014)

Impulse responses of liquidity risk and credit risk (2015-2017)

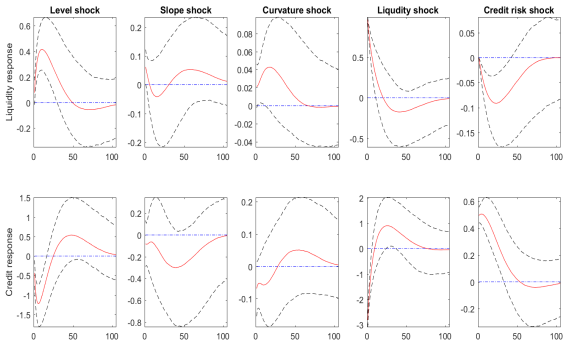


Figure 17: Impulse responses of liquidity risk and credit risk (2015-2017)

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Conclusions (for now)

- Evolving systemic bond market risks from liquidity risk (2009-2014) to credit risk (2015-2017)
- Risks from local public debt significantly affect the Treasury yields: flight to liquidity (2009-2014), flight to safety (2015-2017)
- Systemic risks significantly priced in Treasury bond risk premia
- Further work on jointly model the Treasury yield curve together with multiple Chengtou yield curves with a set of risk factors.